



Rheinische  
Friedrich-Wilhelms-  
Universität Bonn

**Prof. Dr. Maren Bennewitz**

Institut für Informatik  
Abteilung VI  
Humanoid Robots Lab  
Adresse:  
Friedrich-Hirzebruch-Allee 8  
53115 Bonn

## Humanoid Robotics

### Assignment 7

Due **Tuesday, June 17<sup>th</sup>**, before lecture.

#### Object Manipulation and Trajectory Generation:

##### 1. Uncommon Gripper Type from Literature

**(Total: 3 points)**

In the lecture we discussed different types of grippers. Identify one gripper (or end - effector) from the robotics literature that is not a standard 2 - finger parallel - jaw gripper, multi - finger (e.g. 5-finger) hand, or vacuum - based suction cup. (Tip: look for recent conference papers—examples include underactuated “soft” grippers, gecko-adhesive pads, or the ROSE-Gripper as discussed in the lecture):

Please provide:

- Name & Reference:** Full name of the gripper, authors, publication venue, and year.
- Working Principle:** How does it grasp? Describe its actuation method (e.g., rotation-based squeezing, adhesion, compliance, etc.) and key mechanical/fabrication elements.
- What Makes It Uncommon:** Explain why this gripper is “uncommon” compared to typical parallel-jaw or multi-finger hands. Is it the geometry, the materials, the actuation strategy, the contact model, or something else?
- Advantages & Limitations:**
  - List at least two advantages (e.g., gentle compliance, ability to handle highly irregular shapes, reduced hardware complexity).
  - List at least two limitations or challenges (e.g., limited force, sensitivity to surface conditions, speed constraints).
- Application Scenario:** Give one concrete scenario (pick a specific object type or manipulation task) where this gripper would outperform a standard parallel-jaw gripper, and explain why.

##### 2. Friction Cone & Maximum Lifiable Load

**(Total: 4 points)**

Consider a simple planar (2D) parallel-jaw gripper grasping a block of mass  $m$  by pinching it on two opposite faces. Each finger applies a normal force  $F$  perpendicular to the contact surface. The contact between each finger and the block is modeled as a **hard-finger** model. Assume static friction coefficient  $\mu$  between the finger pads and the block.

Consider a block of unknown mass  $m$ , gripped by a parallel-jaw gripper with each finger capable of applying  $F=80\text{N}$ . The fingertip material and the block surface together give  $\mu=0.3$ . Use  $g=9.81\text{m/s}^2$ .

- Compute the half-angle  $\theta$  of the friction cone in degrees.
- Find the maximum frictional force  $f_{t,\max}$  at each finger.



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- c. Determine the maximum mass  $m_{\max}$  that the gripper can lift without slipping.
- d. Suppose the block's actual mass is  $m=2.0\text{kg}$ . Verify whether this gripper can lift it. If not, compute the **minimum** normal force  $F_{\min}$  each finger must apply (for the same  $\mu=0.3$ ) to just barely lift a 2.0kg block.

You can decide if you want to do this exercise in python or pen-and-paper. If you decide for the latter, please upload it as pdf to your solutions.

### 3. Trajectory Interpolation

(Total: 8 points)

In this task, you will implement various trajectory-parameterization schemes for a single- and multi-degree-of-freedom manipulator using the concepts introduced in the Trajectory Generation section of hr06\_manipulation\_2.pdf. Clearly define your functions, document inputs/outputs, and include brief comments explaining your approach. You may use Python and NumPy; plotting libraries (e.g., Matplotlib) are permitted for visualization. Ensure your solutions work for arbitrary number of multiple joints for c and d.

a. Implement a **constant velocity trajectory interpolator** for a single joint that has a maximum joint speed of **90** degrees/s. At  $t=0$ , the joint position is  $\pi$  radians. The goal joint position is **-2.5** radians. At what time will it reach the desired the goal state? Use a cycle time of **0.01** seconds for interpolation. Plot joint position and velocity curves. **(1 point)**

b. Implement a **trapezoidal velocity interpolator** for a joint that has a maximum joint speed of **90** degrees/s and a maximum acceleration of **180** degree/s<sup>2</sup>. It should ensure that when motion duration is too low, it skips the constant velocity phase. Plot the joint position, velocity and acceleration curves for the following two cases. Use a cycle time of **0.01** seconds for interpolation. **(3 points)**

- Initial position = **0** radians, Final position =  $\pi$  radians
- Initial position = **0.1** radians, Final position =  $\pi/4$  radians

c. Extend the **trapezoidal velocity interpolator** for **multiple joints in vectorized fashion**. Calculate the time required and attained peak velocity for each joint to reach its goal. Plot the position, velocity and acceleration curves. Use a cycle time of **0.01** seconds for interpolation. **(2 points)**

| Joint | Initial (radians) | Final (radians) | Maximum Speed (degree/s) | Maximum Acceleration (degree/s <sup>2</sup> ) |
|-------|-------------------|-----------------|--------------------------|---|
| 1     | 0.5               | 2.0             | 45                       | 90  |
| 2     | -0.2              | 0.4             | 90                       | 90  |
| 3     | 1.0               | 0.5             | 30                       | 90  |

d. Now implement **synchronized multi-joint trapezoidal velocity interpolator** so that all joints reach the final position at the same time. Plot the position, velocity and acceleration curves. Use a cycle time of **0.01** seconds for interpolation for the example given in c. Compare and contrast c vs d using the plotted curves and explain which one is preferred and why. **(3 points)**